

---

# Summary of activities in NLO multi-leg/NNLO working group



June 29, 2007

# Les Houches 07 wishlist

process ( $V \in \{Z, W, \gamma\}$ )	# groups working on
1. $pp \rightarrow V V \text{ jet}$	$\sim 4$
2. $pp \rightarrow t\bar{t} b\bar{b}$	$\sim 1$
3. $pp \rightarrow t\bar{t} + 2 \text{ jets}$	
4. $pp \rightarrow W W W$	$\sim 2$
5. $pp \rightarrow V V b\bar{b}$	
6. $pp \rightarrow V V + 2 \text{ jets}$	
7. $pp \rightarrow V + 3 \text{ jets}$	$\sim 2$
8. $pp \rightarrow b\bar{b}b\bar{b}$	$\sim 1$
9. $pp \rightarrow 4 \text{ jets}$	$\sim 1$ (theor. interest)
10. $gg \rightarrow W^*W^*$ (NLO, 2 loops)	$\sim 1$
11. NNLO for $t\bar{t}$	$\sim 1$
12. NNLO for $Z/\gamma + \text{jet}$	(gluon pdfs)

# progress

---

- change in philosophy:  
more automatisisation/modular tools

# progress

---

- change in philosophy:  
more automatisisation/modular tools
- better methods:
  - learn, discuss, compare
  - "what is a good method depends on the type of the problem"

# "new" approaches

---

- General introduction to "new directions for one-loop calculations" (Zoltan Kunszt)

# "new" approaches

---

- General introduction to "new directions for one-loop calculations" (Zoltan Kunszt)
- Introduction to on-shell recursion for tree level amplitudes (Ruth Britto)  
joint with BSM group!

# "new" approaches

---

- General introduction to "new directions for one-loop calculations" (Zoltan Kunszt)
- Introduction to on-shell recursion for tree level amplitudes (Ruth Britto)  
joint with BSM group!
- Unitarity constructions for one-loop amplitudes (4-dim and D-dim  $\Rightarrow$  rational parts) (Ruth Britto)

# "new" approaches

---

- General introduction to "new directions for one-loop calculations" (Zoltan Kunszt)
- Introduction to on-shell recursion for tree level amplitudes (Ruth Britto)  
joint with BSM group!
- Unitarity constructions for one-loop amplitudes (4-dim and D-dim  $\Rightarrow$  rational parts) (Ruth Britto)
- Reconstruction of coefficients of one-loop master integrals and of the rational terms by solving a system of equations numerically (Costas Papadopoulos)



# "new" approaches

---

- General introduction to "new directions for one-loop calculations" (Zoltan Kunszt)
- Introduction to on-shell recursion for tree level amplitudes (Ruth Britto)  
joint with BSM group!
- Unitarity constructions for one-loop amplitudes (4-dim and D-dim  $\Rightarrow$  rational parts) (Ruth Britto)
- Reconstruction of coefficients of one-loop master integrals and of the rational terms by solving a system of equations numerically (Costas Papadopoulos)
- "The magic of cut-construction" (Zvi Bern)  
complex momenta are the key to new solutions  
(and new pitfalls)  
"unreal" poles can cause "real" headaches

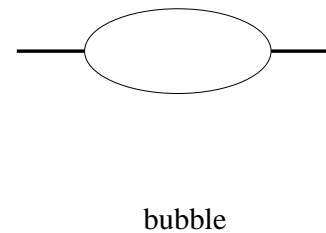
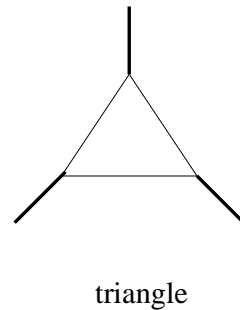
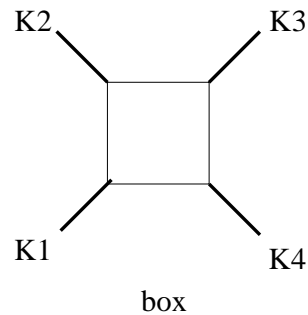
---

## Master Integrals

Passarino-Veltman reduction brings the one-loop amplitude to the form

$$A_{n;1} = \sum_i d_i (\text{box}) + \sum_i c_i (\text{triangle}) + \sum_i b_i (\text{bubble}) + \text{rational}$$

where expressions for scalar bubble, scalar triangle and scalar box integrals are known explicitly. (in dim. reg.: Bern, Dixon, Kosower )



# Les Houches Accord on MI's

---

needed by most of the approaches:

**one-loop master integrals**

**Les Houches accord on Master Integrals:**

- agreement on format to uniquely characterise the integral (LoopTools conventions)
- **WIKI page** where everybody can post previously unknown MI's
- hosted at <http://durpdg.dur.ac.uk/hepdata/>

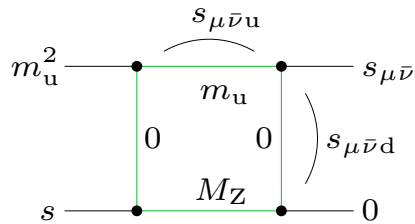
# semi-numerical approaches

---

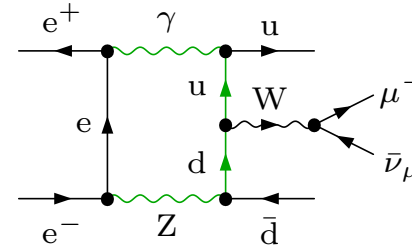
- Techniques for multi-leg one-loop tensor integrals (Ansgar Denner)
  - detailed discussion of numerical stability issues ( $\det(\text{Gram}) \rightarrow 0, \det(\text{Cayley}) \rightarrow 0, \text{both dets} \rightarrow 0$ )
  - "phase space integration reveals weaknesses of methods"

A very delicate example with small Gram and mod. Cayley determinants:

Box integral

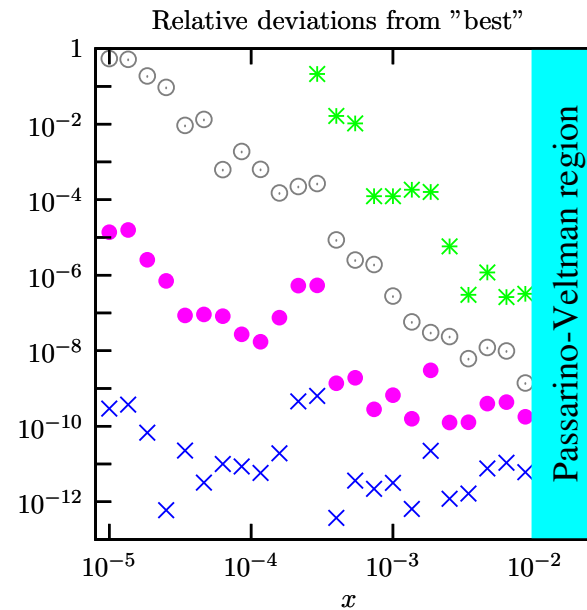
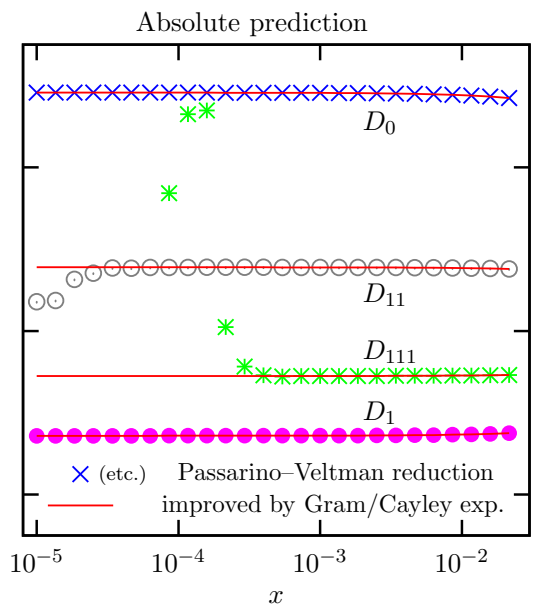


appears, e.g., in subgraph of diagram



Gram det.:  $\det(Z), \det(X) \rightarrow 0$  if  $s_{\mu\bar{\nu}d} \rightarrow s$  and  $s_{\mu\bar{\nu}u} \rightarrow s_{\mu\bar{\nu}}$

Numerical comparison: maximal tensor rank = 25



$$x \equiv \frac{s_{\mu\bar{\nu}d}}{s} - 1$$

$$\equiv \frac{s_{\mu\bar{\nu}u}}{s_{\mu\bar{\nu}}} - 1$$

$$s = 4 \times 10^4 \text{ GeV}^2$$

$$s_{\mu\bar{\nu}} = 64 \times 10^2 \text{ GeV}^2$$

PV reduction breaks down,  
but Gram/Cayley exp. stable  
for  $\det(Z), \det(X) \rightarrow 0$ !

# Phenomenological results

---

- $pp \rightarrow t \bar{t}$  jet production (Peter Uwer)
- $pp \rightarrow V V j j$  via VBF (Dieter Zeppenfeld)
- Electroweak corrections to gauge boson production at high  $p_T$  (Stefano Pozzorini)  
 $pp \rightarrow VV'$ , differences to massless gauge theories, discussion of real W/Z emission
- EW (and QCD) corrections to Hjj production via VBF (Ansgar Denner)

---

Recent studies for  $pp \rightarrow VV'$

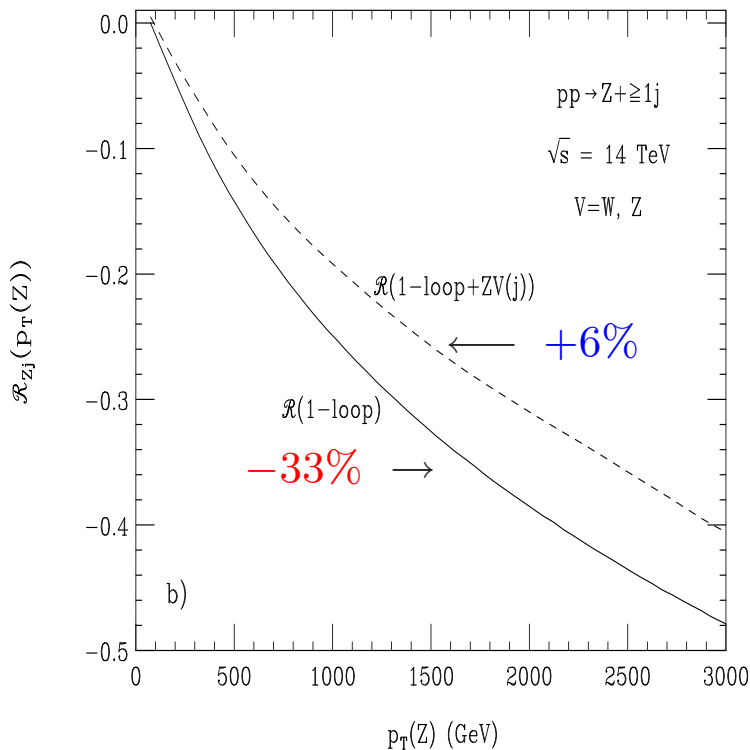
- all processes apart from  $pp \rightarrow \gamma\gamma$  computed

process	decay	hard $\gamma$	corrections	
$W\gamma, WZ$	yes	no	NLL	<a href="#">Accomando, Denner, S.P. (2002)</a>
$Z\gamma$	no	yes	exact	<a href="#">Hollik, Meier (2004)</a>
$WW, WZ, ZZ$	yes	yes	NLL	<a href="#">Accomando, Denner, Kaiser (2005)</a>
$W\gamma, Z\gamma$	yes	yes	exact+NLL	<a href="#">Accomando, Denner, Meier (2005)</a>

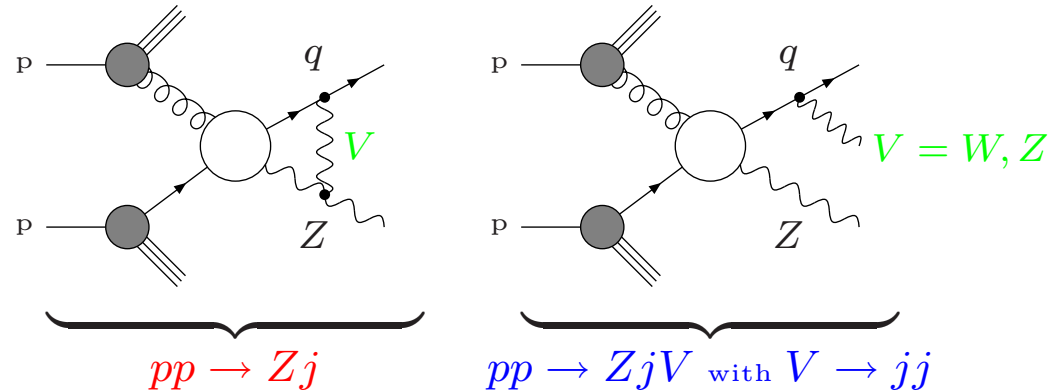
- similar conclusions as for  $W\gamma, WZ$

## Real W and Z emission for $pp \rightarrow Zj$ [Baur (2006)]

“ Since the number of jets is not fixed in a measurement of the  $Z$  boson  $p_T$  distribution,  $\mathcal{O}(\alpha_s \alpha^2)$   $ZVj$  production with  $V \rightarrow jj$  has to be included when calculating weak radiative corrections ”



### Virtual and real $\mathcal{O}(\alpha)$ corr. to $pp \rightarrow Zj$



- $W, Z$  emission can be non-negligible and partially cancel EW virtual corrections
- depends on observable definition and can be reduced by jet veto



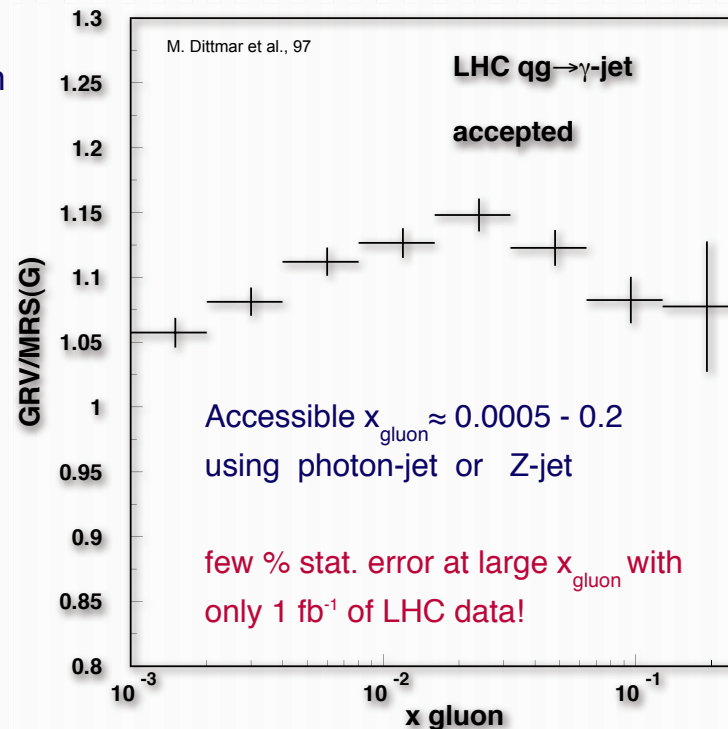
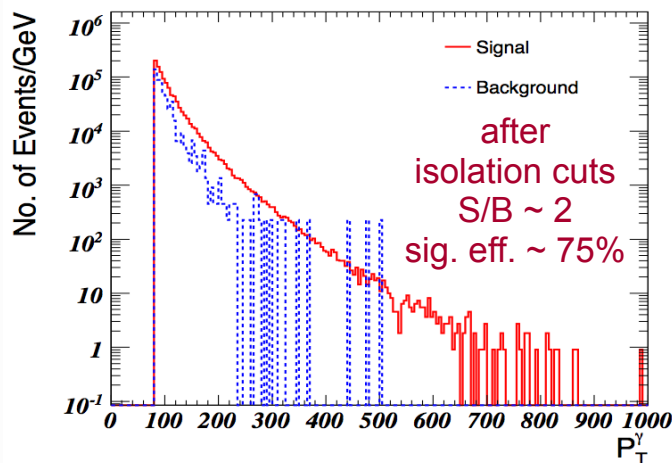
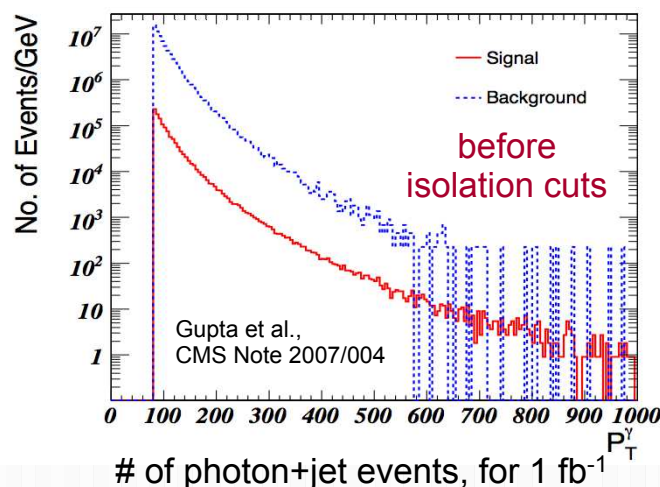
# NNLO corrections

---

- Expected uncertainties at the LHC (Günther Dissertori)

## Prompt Photon Production

- it's all about isolation
- reduce background by combination of isolation requirements using Tracker, ECAL and HCAL



- constrain gluon pdf
- energy scale well controlled by photon
- other issues there:  
interplay real radiation - fragmentation
- Z+jet : smaller rate, best possible prediction needed

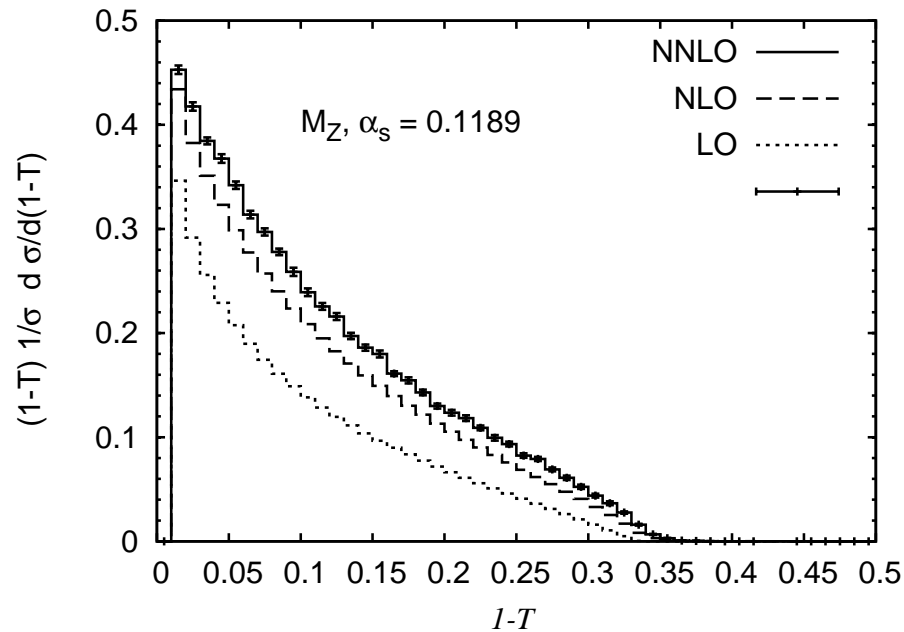
# NNLO corrections

---

- Expected uncertainties at the LHC (Günther Dissertori)
- $e^+e^- \rightarrow 3$  jets at NNLO (Aude Gehrmann-De Ridder)  
initiated at Les Houches '01 ... 6 years  
of man-and woman-power!

# Results

## The thrust distribution



- errors are numerical
- comparison with data ongoing
- visible enhancement due to NNLO contributions (15 %)

# NNLO corrections

---

- Virtual corrections for  $pp \rightarrow t\bar{t}$  production at NNLO  
(Michael Czakon)

## Direct computation

- Statistics
- annihilation channel
  - 190 diagrams expressed through 2812 integrals
  - 145 master integrals in the full result
  - 69 master integrals needed in the present calculation
- fusion channel
  - 726 diagrams expressed through 8676 integrals
  - 422 master integrals in the full result
  - 174 master integrals needed in the present calculation

---

## Publicly available Software

- MB.m package (MC) written in MATHEMATICA
    - FORTRAN interface for numerics
    - CUBA library for integration
    - CERNlib for Gamma functions
- <http://theorie.physik.uni-wuerzburg.de/~mczakon>  
MC, Comput.Phys.Commun.175:559-571,2006.
- Basic functionality
    - MBoptimizedRules : determination of contours
    - MBcontinue : analytic continuation
    - MBexpand : expansion in a chosen parameter (e.g. Epsilon)
    - MBintegrate : numerical integration for specified kinematics
  - Input
    - Mellin-Barnes representation
  - Useful external software
    - AMBRE (Automatic Mellin-Barnes Representations)  
Gluza, Kajda and Riemann
    - XSummer (evaluation of harmonic sums) S. Moch and P. Uwer

---

# Private software components for generic computations

- C++ library DiaGen (9.700 lines of code)
  - topology and diagram generation
  - topological isomorphism and symmetry groups
  - integral identification
  - QFT topological properties+ 1100 lines of Utilities library
- C++ library IdSolver (9.600 lines of code)
  - solution of identity systems between integrals
  - simplification by topological analysis
  - handling of large databases
- Mathematica packages for Mellin-Barnes integrals (8.200 lines of code)
  - generation of representations from Feynman integrals
  - analytic continuation and numerical evaluation
  - expansion in small parameters
  - application of Barnes lemmas
  - conversion to nested sums and resummation by PSLQ



- 
- **HNNLO**: Fully differential program for Higgs production at NNLO (Massimiliano Grazzini)

## An example: $gg \rightarrow H \rightarrow \gamma\gamma$

Use cuts as in CMS TDR

$$p_T^{\min} > 35 \text{ GeV}$$

$$p_T^{\max} > 40 \text{ GeV} \quad |y| < 2.5$$

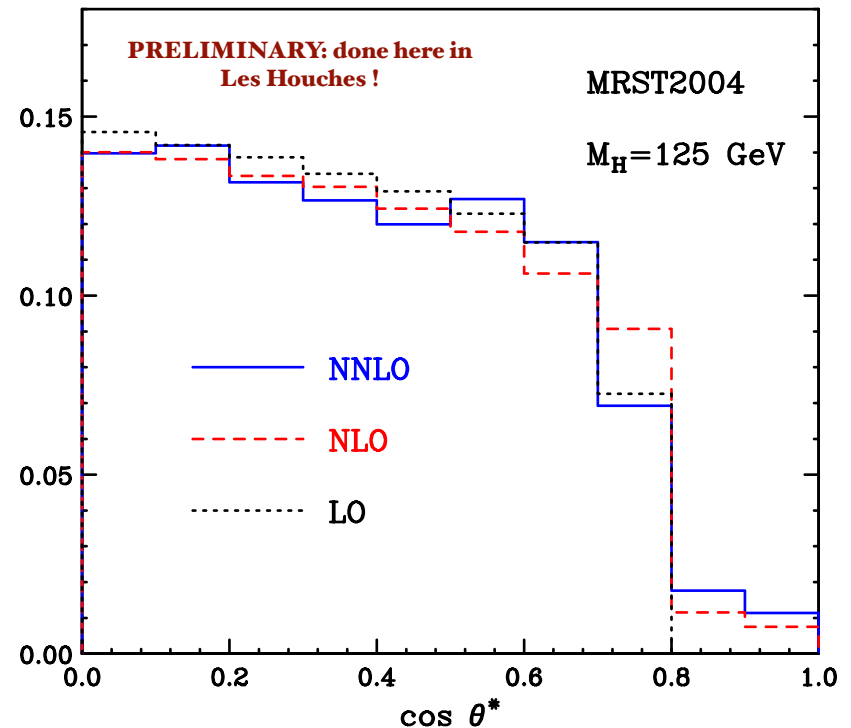
Photons should be isolated:  
total transverse energy in a  
cone of radius  $R = 0.3$  should  
be smaller than 6 GeV

**define**  $\cos \theta^*$  **distribution**

$\theta^*$  **polar angle of one of the  
photons in the Higgs rest frame  
(used by ATLAS:  
thanks to Suzanne Gascon and  
to Markus Schumacher)**

note upper bound on  $\cos \theta^*$  at LO

→ again perturbative instability  
beyond LO !



# Outlook

---

After all these efforts ...

we are eager to compare to **data** at

**Les Houches 2009 !**