
What has been achieved since Les Houches 2005 ?

What has been done in session 1 ? NLO multi-leg group

Gudrun Heinrich



Les Houches 05: NLO wishlist for LHC

process ($V \in \{Z, W, \gamma\}$)	background to
1. $pp \rightarrow V V \text{ jet}$	$t\bar{t}H$, new physics
2. $pp \rightarrow H + 2 \text{ jets}$	H production by VBF
3. $pp \rightarrow t\bar{t} b\bar{b}$	$t\bar{t}H$
4. $pp \rightarrow t\bar{t} + 2 \text{ jets}$	$t\bar{t}H$
5. $pp \rightarrow V V b\bar{b}$	VBF $\rightarrow H \rightarrow VV$, $t\bar{t}H$, new physics
6. $pp \rightarrow V V + 2 \text{ jets}$	VBF $\rightarrow H \rightarrow VV$
7. $pp \rightarrow V + 3 \text{ jets}$	various new physics signatures
8. $pp \rightarrow V V V$	SUSY trilepton

achieved (from wishlist):

● $pp \rightarrow H + 2 \text{ jets}$ Campbell, Ellis, Giele, Zanderighi '05/06

● $pp \rightarrow Z Z Z$ Lazopoulos, Melnikov, Petriello '07

● $\mathcal{O}(\alpha^6 \alpha_s)$:

$pp \rightarrow Z Z + 2 \text{ jets}$ via VBF,

$pp \rightarrow W W + 2 \text{ jets}$ via VBF,

$pp \rightarrow W Z + 2 \text{ jets}$ via VBF

Jäger, Oleari, Zeppenfeld '06

Bozzi, Jäger, Oleari, Zeppenfeld '07

Les Houches 07 wishlist

process ($V \in \{Z, W, \gamma\}$)	# groups working on
1. $pp \rightarrow V V \text{ jet}$	2
2. $pp \rightarrow t\bar{t} b\bar{b}$	1
3. $pp \rightarrow t\bar{t} + 2 \text{ jets}$	
4. $pp \rightarrow W W W$	1 (?)
5. $pp \rightarrow V V b\bar{b}, V V t\bar{t}$	
6. $pp \rightarrow V V + 2 \text{ jets}$	
7. $pp \rightarrow V + 3 \text{ jets}$	
8. $b\bar{b}b\bar{b}$	1
9. $gg \rightarrow W^*W^*$ (NLO, 2 loops)	?
10. EW corrections to VBF	1
11. NNLO to VBF, $t\bar{t}$, $Z/\gamma+\text{jet}$, $W+\text{jet}$?

That's all ???

NO!

- processes which were not on the wishlist

examples: (SM, LHC kinematics only, $N > 4$ only)

- $pp \rightarrow t\bar{t} + \text{jet}$ Dittmaier, Uwer, Weinzierl '07
- $pp \rightarrow Z + 2 \text{ jets}, W + 2 \text{ jets with one } b\text{-quark tag}$
Campbell, Ellis, Maltoni, Willenbrock '06, '07
- $pp \rightarrow H b\bar{b}$ Febres Cordero, Reina, Wackerath '06
- $pp \rightarrow H H H$ Plehn, Rauch '05; Binoth, Karg, Kauer, Rückl '06
- ...

progress

- important new technical developments
 - analytic methods (twistor/string inspired)
 - Zoltan's talk this afternoon,
 - Ruth Britto's talk next week

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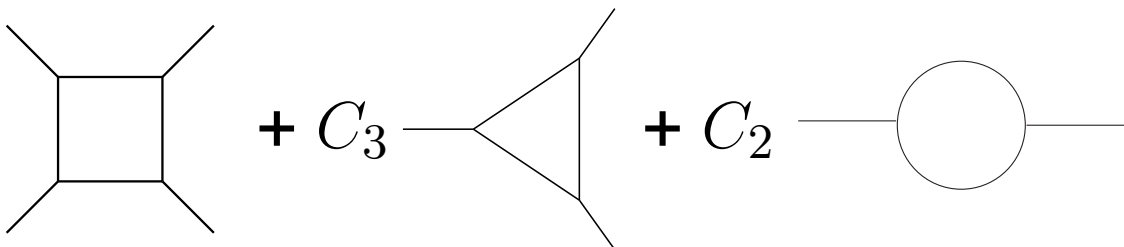
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 - tensor reduction \Rightarrow set of "basis integrals":
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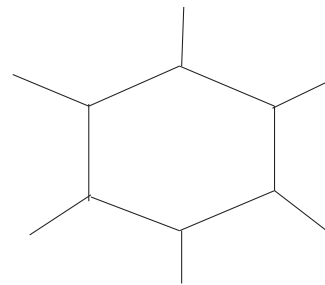
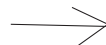
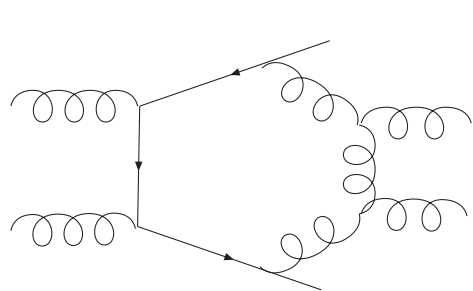
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$$A = C_4 \text{ (box diagram)} + C_3 \text{ (triangle diagram)} + C_2 \text{ (bubble diagram)} + \mathcal{R}$$


The equation shows the decomposition of an amplitude A into a sum of Feynman diagrams. The first term is a box diagram with four external lines. The second term is a triangle diagram with three external lines. The third term is a bubble diagram with two external lines. The fourth term is a remainder term R.

tensor reduction

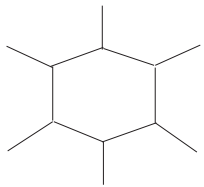


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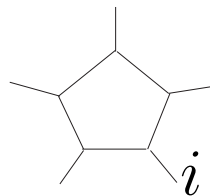
integrals with less legs
from reduction of tensor rank and
number of legs at the same time

non-trivial tensor structure

scalar 6-point function



$$= \sum_{i=1}^6 b_i$$



...

factorial growth in complexity !

(semi-)numerical methods cont'd.

possible solutions:

- do tensor reduction (partly) numerically
Campbell, Ellis, Giele, Zanderighi; Denner, Dittmaier, Uwer, Weinzierl;
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- solve system of equations which determines coefficients of basis integrals numerically
Papadopoulos, Pittau, Ossola; Ellis, Giele, Kunszt

technical developments cont'd.

- **fully numerical methods:**
do integration over loop momenta and/or Feynman parameters numerically
problem: **isolation of singularities**
Anastasiou, Beerli, Daleo, Kunstz; Ferroglia, Passera, Passarino, Uccirati;
Lazopoulos, Melnikov, Petriello; Krämer, Nagy, Soper; Kurihara, Kaneko, ...
- **improved methods for real radiation at NLO**
(partly inspired by NNLO efforts)
Daleo, Gehrmann, Maître; Nagy, Somogyi, Trocsanyi;
Weinzierl, Schwinn, Gleisberg, ...

superficial comparison of methods

● analytic methods

- + compact expressions
- + evaluation of analytic expressions fast
- processes with massive particles in the loop and/or many different mass scales difficult
- automatisisation in its infancy, numerical behaviour not yet studied sufficiently

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- + automated processing can make use of already existing "industry"
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● numerical methods

- + do not generate large analytic expressions
- numerical integration in multi-dimensional parameter space with intricate pole structure non-trivial

towards NLO 2 \rightarrow 4 scattering

6-point results achieved:

- complete one-loop amplitudes for
 - 6 gluons
Britto, Feng, Mastrolia; Ellis, Giele, Zanderighi;
Berger, Bern, Dixon, Dunbar, Forde, Kosower; Xiao, Yang, Zhou;
Bedford, Brandhuber, Spence, Travaglini;
Britto, Buchbinder, Cachazo, Feng, ... '94-'06
 - 6 photons
Nagy, Soper; Binoth, Gehrmann, GH, Mastrolia;
Papadopoulos, Ossola, Pittau; Forde '06/07
- full electroweak corrections to $e^+e^- \rightarrow 4f$
Denner, Dittmaier, Roth, Wieders Feb. 05, but should be mentioned
- $e^+e^- \rightarrow HH\nu\bar{\nu}$
GRACE group (Boudjema et al.) 10/05

- important developments towards **matching NLO with parton showers**

Frixione, Nason, Webber, . . . , Nagy, Soper, . . . , Giele, Kosower, Skands, Krämer, Mrenna, . . . , Gieseke, Latunde-Dada, Ridolfi, . . . , Gleisberg, Höche, Krauss, Schälicke, Schumann, Winter, . . .

enormous activity in session 1

- resummation:

- H production, doubly differential in q_T and y
Bozzi, Catani, DeFlorian, Grazzini '07

- single-inclusive jet production near threshold
DeFlorian, Vogelsang '07

- . . .

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 - important topic in session 1:
can we achieve high level of **modularity** to compare/exchange pieces of code which are common to many approaches?
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 - some kind of "**Les Houches Accord**" on input/output ?

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achieved in session 1 ...

Les Houches Accord on Master Integrals

needed by most of the approaches:

one-loop master integrals

Les Houches accord on Master Integrals:

- agreement on format to uniquely characterise the integral (LoopTools conventions)
- **WIKI page** where everybody can post previously unknown MI's
- hosted at <http://durpdg.dur.ac.uk/hepdata/>
(put up by Jeppe Andersen)

automatisation/modularity

- one-loop tensor integrals:

Keith Ellis suggested to provide (public) code for one-loop **tensor** integrals with massless internal lines up to rank 5 pentagons

- real radiation:

T. Gleisberg is working on a code (**to be made public**) for **automated** generation of **dipole subtraction** terms

to be addressed during this workshop

- How can "string inspired/standard approaches" maximally profit from each other?
 - make use of **complementarity** of different approaches
 - assess limitations and future prospects of "traditional/new" approaches
 - discuss in particular **rational parts**, **massive** loops
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agreement in session 1:

dedicated section on **rational parts** in the proceedings

topics to be addressed

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- **numerical stability** in NLO multi-leg calculations:
classify **types of singularities** which can occur in an amplitude

Numerical Stability



"Numerical instabilities are like bad spots on an apple"
(Dave Soper)

Singularities in scattering amplitudes

questions:

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(are they always at the phase space boundaries?)

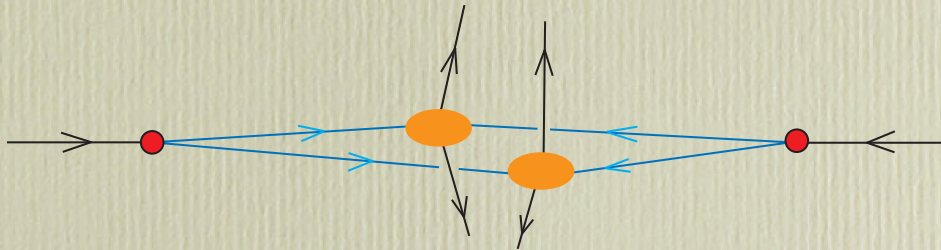
Singularities in scattering amplitudes

questions:

- where do the bad spots come from? (which type of singularity?)
- are they only on the surface of the apple?
(are they always at the phase space boundaries?)
- if I make an apple cake:
(integrate the amplitude over the phase space)
 - are the spots harmless? (integrable?)
 - can I cut out the bad spots and still have enough apple left for the cake? (to drop or interpolate problematic phase space points: do they represent a negligible fraction of phase space?)
 - if I cut the cake, do hidden bad spots suddenly show up? (how do kinematic cuts affect the numerical stability?)

disadvantages ...

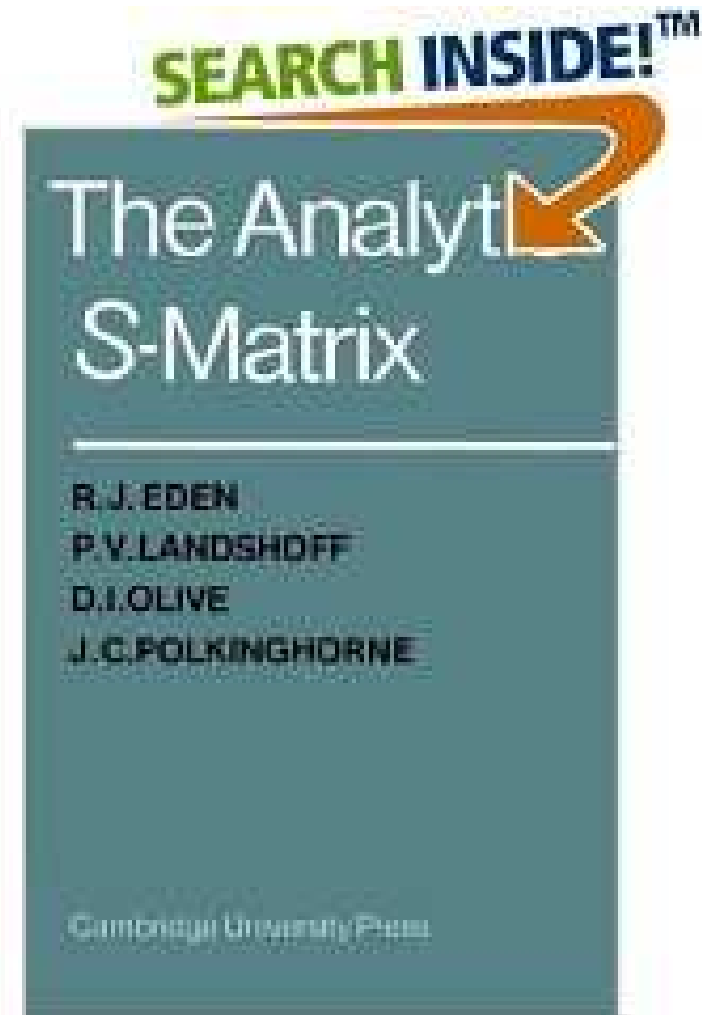
- There can be problems from double parton scattering singularities.



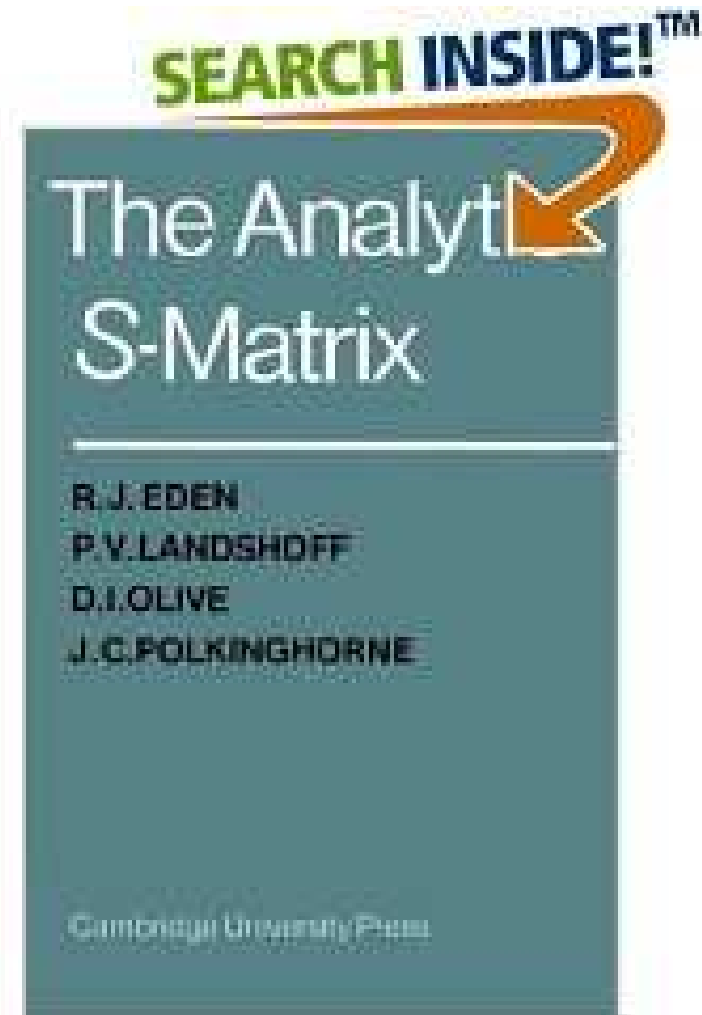
- This starts at $N = 6$.

Z.Nagy

Revenge of the Analytic S-matrix



Revenge of the Analytic S-matrix



translate the Bible
into modern language !

extra slides

Numerical Stability

- **plan**: dedicated section in the proceedings on different types of singularities (Giele, Duplancic, et al)
- **agreement** on information that would be useful in a publication:
 - amplitudes in analytical form: give **numerical value** at certain phase space point(s) such that others can compare
 - integrated amplitudes/cross sections: statements about **numerical behaviour**
 - what fraction of phase space shows instabilities ?
 - how have they been dealt with ?

Virtual Corrections

... interference of LO diagrams with

$$\begin{aligned}
 \mathcal{M}_V = & \text{[Diagram 1]} + \text{[Diagram 2]} + \text{[Diagram 3]} + \dots \\
 = & \mathcal{M}_B F(Q) \left[-\frac{2}{\epsilon^2} - \frac{3}{\epsilon} \right] + \tilde{\mathcal{M}}_V^{finite}
 \end{aligned}$$

$\tilde{\mathcal{M}}_V^{finite}$ computed with Passarino-Veltman reduction
 cumbersome: (numerically small) **pentagon** contributions

combination of real emission and virtual contributions with
 subtraction terms according to dipole approach of
Catani & Seymour

poles canceled analytically \rightarrow **finite** results